

Instructions: Complete each of the following on separate, stapled sheets of paper.

1. Use the definition of the Laplace transform to compute $\mathcal{L}\{f(t)\}$ for each function below.

(a) $f(t) = e^{t+7}$

(c) $f(t) = t \cos(t)$

(b) $f(t) = e^{-t} \sin(t)$

(d) $f(t) = t^2 e^{-2t}$

2. Compute the Laplace transform of the following functions using the table of Laplace transforms.

(a) $f(t) = 2t^4$

(c) $f(t) = (e^t + e^{-t})^2$

(b) $f(t) = 7t^5 + 3t$

(d) $f(t) = \cos(5t) + \sin(3t)$

3. Compute the inverse Laplace transform for each of the following functions $F(s)$.

(a) $F(s) = \frac{1}{s^3}$

(d) $F(s) = \frac{1}{s^2 + s - 20}$

(b) $F(s) = \frac{(s+1)^3}{s^4}$

(e) $F(s) = \frac{1}{s^3 + 5s}$

(c) $F(s) = \frac{2s-6}{s^2+9}$

(f) $F(s) = \frac{s-3}{s^2-3}$