

The following is a list of topics we have covered over the course of the semester.

1. Basic Logic
  - (a) propositions, connectives, and logical equivalence
  - (b) predicates and quantifiers
  - (c) rules of inference and natural deduction
2. Naïve Set Theory
  - (a) basic operations: union, intersection, set difference, Cartesian product
  - (b) subsets and set equality
3. Basic Number Theory
  - (a) divisibility, its basic properties, and modular arithmetic
  - (b) greatest common divisors and Euclid's Algorithm
  - (c) prime numbers and the Fundamental Theorem of Arithmetic
4. RSA Cryptography
5. Mathematical Induction and Recursion
6. Enumeration
  - (a) Sum Principle, Product Principle, Correspondence Principle, and Inclusion-Exclusion
  - (b) binomial coefficients and the Binomial Theorem
  - (c) the Pigeonhole Principle
7. Functions and Relations
  - (a) functions: injective, surjective, and bijective
  - (b) relations: reflexive, symmetric, antisymmetric, and transitive
  - (c) equivalence relations
8. Graph Theory
  - (a) the Handshake Lemma
  - (b) subgraphs, connection, and coloring
  - (c) Eulerian and Hamiltonian cycles
9. Trees
  - (a) characterizations involving acyclicity and connectedness
  - (b) spanning trees
  - (c) the Prüfer code
10. Models of Computation
  - (a) finite state machines, deterministic/nondeterministic finite state automata
  - (b) language recognition and finite state automata